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# Carbon Revenue Redistribution Strategies In Deregulated Power Markets

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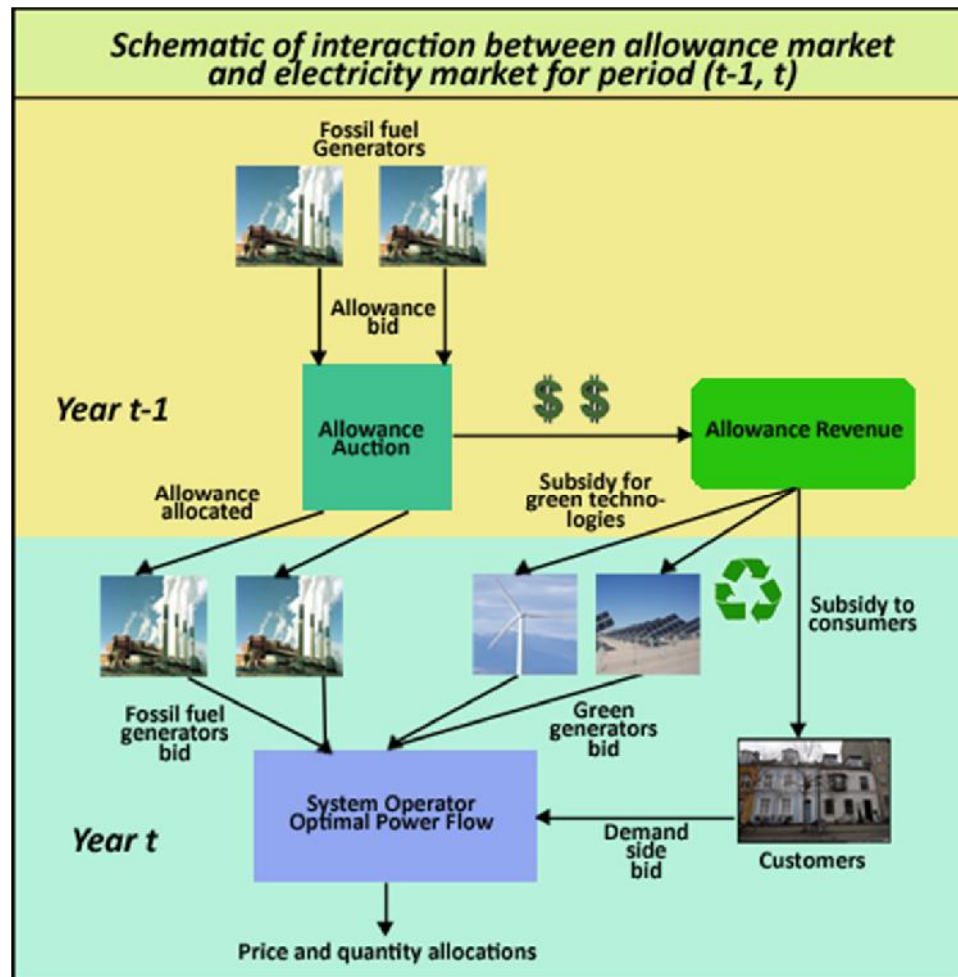
# Motivation

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- Carbon revenue redistribution is a feature common to cap-and-trade and carbon tax programs
- Amount of money collected would be significant (estimated \$69 to \$126 billion in first 5 years)
  - This is a new source of revenue
- Economists have argued in favor of redistributing the revenue to mitigate potential negative economic impact



# Market Schematic



# Potential Recipients

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- Households (consumers)
  - Why? Electricity companies will pass on to the consumers the cost of allowances/carbon tax
  - \$1,158 to \$4,119 extra (in 1999 dollars) per household
- Low emission generators
  - Why? Need to increase market share of low-emission generators if emissions reductions are to be achieved
  - Targets for renewable based generation (EU 21%)



# Literature (Households)

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- Lump sum redistribution
  - Barnes and Breslow (2001)
- Reduction of distortionary taxes
  - Goulder (1995), Parry and Bento (2000)
- Lump sum redistribution more helpful for low-income families
  - Dinan and Rogers (2002)



# Literature (low-emission gencos)

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- Common in U.K., Denmark, Japan, Netherlands, among others
- Bills in the U.S. Congress have started considering these subsidies
  - Cantwell bill considers 25% of carbon revenue earmarked for clean energy investments
- Connecticut (RGGI Member) considers 23% of allowance auction revenue to support renewable energy programs



# Our Model

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- We consider:
  - Bid subsidies for low-emission generators
    - To lower consumer prices across the network
  - R & D subsidies for low-emission generators
    - To encourage sustained cost reduction for low-emission technologies (PV, wind, biomass, geothermal)



# Our Model (continued)

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## Considers

- network constraints via Optimal Power Flow (OPF)
- multi-year horizon
- cap-and-trade (or carbon tax) implemented on a defined geographical region
- regional equity issues related to the “equal per capita redistribution rule”





# Types of Subsidies

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- Bid subsidies
  - Effect is realized during current year
- R & D subsidies
  - Effect is realized throughout the planning horizon
  - Knowledge stock is a function of cumulative stock (investment)  $Y$  of R & D
$$K(Y^t) = \left(\frac{Y^{t-1}}{Y^0}\right)^\beta \text{ (Fischer and Newell, 2008)}$$
  - The impact of knowledge stock on production cost  $C$  is given by  $K^{-1}C$



# Types of Subsidies and OPF

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- R & D subsidies

- We define the reduction on production cost as:

$$R = C - K^{-1}C$$

- Since the above expression is non-linear, we use a least squares approximation as

$$\hat{R} = \alpha K$$

where  $\alpha$  is the regression coefficient



# Mathematical Formulation

$$\max \sum \left[ \text{Benefit to consumers} - \sum_t \sum_h \sum_j \left( \text{Cost to fossil-fuel generators} \right) - \sum_t \sum_h \sum_k \left( \text{Cost to green generators} \right) \right], \quad (1) \quad \text{Social Welfare Function}$$

subject to:

$$Q_h^t - D_h^t - \sum_{l \in I(h)} (m_{hl}^t - m_{lh}^t) = 0 \quad \forall \text{ node } h, t \quad (2)$$

$$\sum_{hl \in A(v)} R_{hl}^t (m_{hl}^t - m_{lh}^t) = 0 \quad \forall \text{ voltage loop } v, t \quad (3)$$

$$Y_{kh}^t - Y_{kh}^{t-1} - y_{kh}^t = 0 \quad \forall k, h, t \quad (4)$$

$$Y_{kh}^T \geq \beta_{kh} \quad \forall k, h \quad (5)$$

$$\sum_h \sum_k q_{kh}^t s_{kh}^t + \sum_h \sum_k y_{kh}^t \leq Z^t \quad \forall t \quad (6)$$

$$m_{hl}^t \leq M_{hl}^t \quad \forall \text{ arc } hl, t \quad (7)$$

$$m_{hl}^t \geq 0 \quad \forall \text{ arc } hl, t \quad (8)$$

$$q_{jh}^t \leq Q_{jh}^t \quad \forall j, h, \quad q_{kh}^t \leq Q_{kh}^t \quad \forall k, h \quad (9)$$

$$q_{jh}^t, q_{kh}^t \geq 0 \quad \forall j, k, h \quad (10)$$

} Kirchhoff's laws Constraints  
 } Cumulative R&D Constraints  
 } Target R&D Constraints  
 } Yearly revenue Constraints  
 } Transmission Constraints  
 } Generation Constraints



# Mathematical Formulation

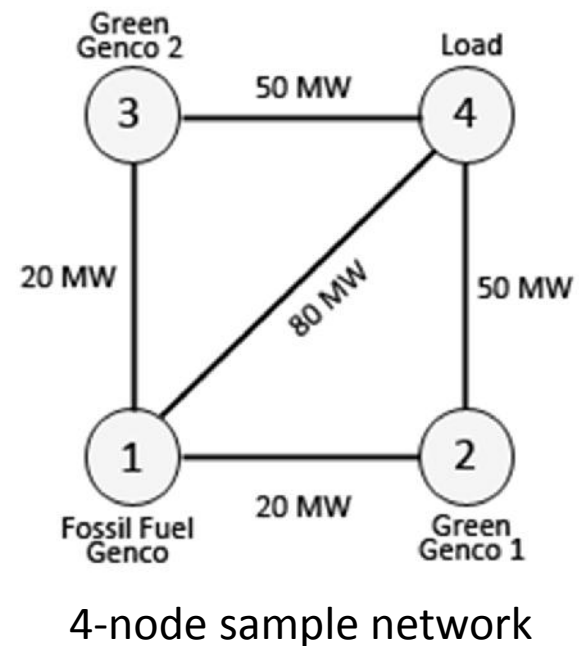
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- Objective function
  - Quadratic, non-convex
- Solved using
  - CONOPT3, MINOS, KNITRO



# Model Application

- 4-node sample network
- Planning horizon: 5 years
- 2 low emission generators
- 1 fossil fuel generator
- 1 load



# Application

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- 2 scenarios
  - discriminatory subsidies
  - non-discriminatory subsidies
- Allowance market scenario
  - perfectly competitive
  - allowances are sold at \$3.38 in year 1
  - this price is increased 10% each year



# Application

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- Initial bidding parameters

Genco	$e$ (\$/MWh)	$f$ (\$/MWh <sup>2</sup> )
Fossil Fuel	10.524	0.05
Green Genco 1	22	0.05
Green Genco 2	24	0.05
Load	$a$	$b$
Load 1	27	0.05

Initial bidding parameters

- R&D learning factors  $\alpha_1=0.005176$ ,  $\alpha_2=0.006878$

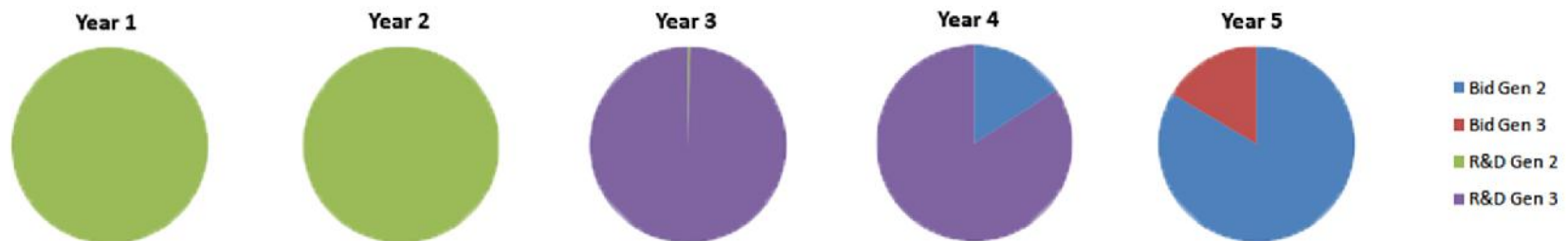
Recall that reduction in production cost (due to subsidies)

is given by  $\hat{R} = \alpha K$



# Results

- Discriminatory subsidies Scenario



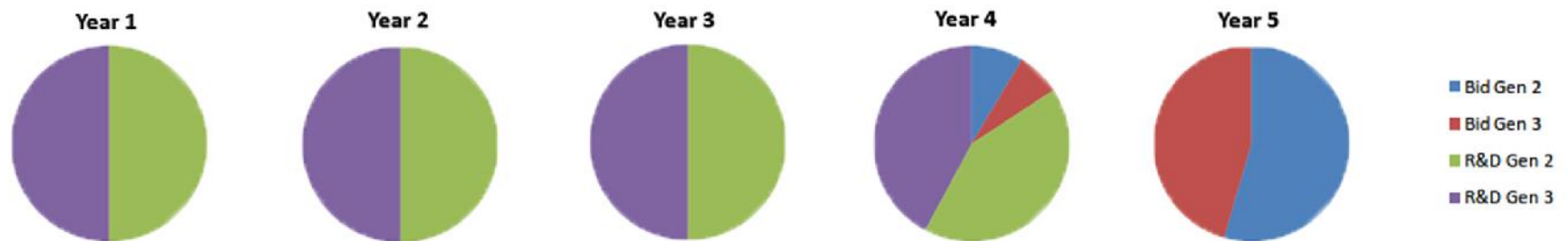
- R&D subsidies are allocated earlier, bid subsidies later, when fossil fuel bids are higher
- R&D subsidies for genco 2 are distributed earlier even though its  $\alpha$  is lower





# Results

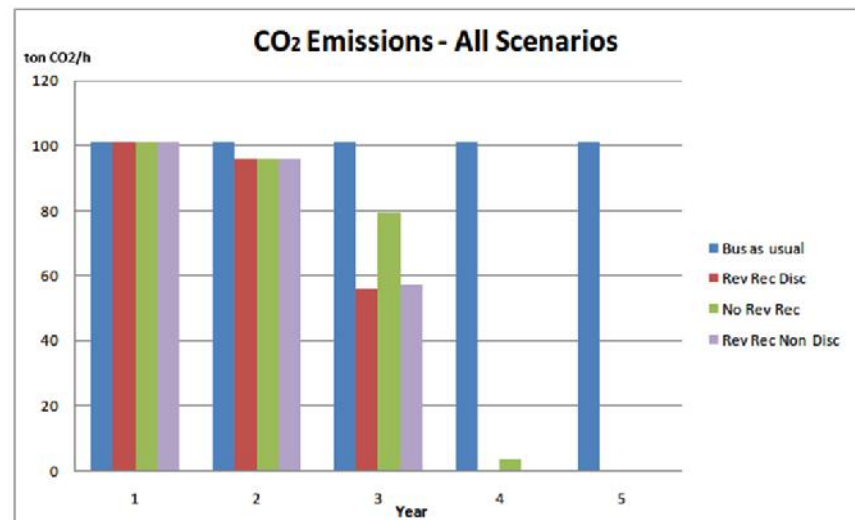
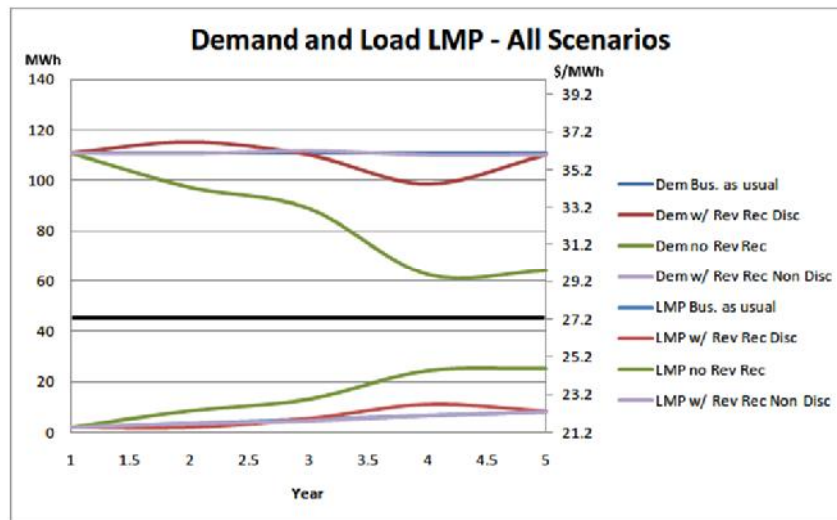
- Non-discriminatory subsidies Scenario



- R&D subsidies continue to be allocated earlier. Bid subsidies later
- Increased fairness in revenue redistribution at the expense of reduced total social welfare
- Since genco 2 produces more, total subsidies for genco 2 are higher



# Results – All scenarios



Revenue recycling prevents demand from decreasing significantly without increasing carbon emissions and prices.



# Summary

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- We have developed a mathematical model for redistributing carbon revenue in a deregulated electricity market.
- In the example problem,
  - R&D subsidies are distributed earlier
  - location of generators in network plays a role in amount of subsidies allocated
  - revenue recycling strategy can be used to mitigate demand reduction without increasing emissions and prices



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Thank you.  
Questions?

